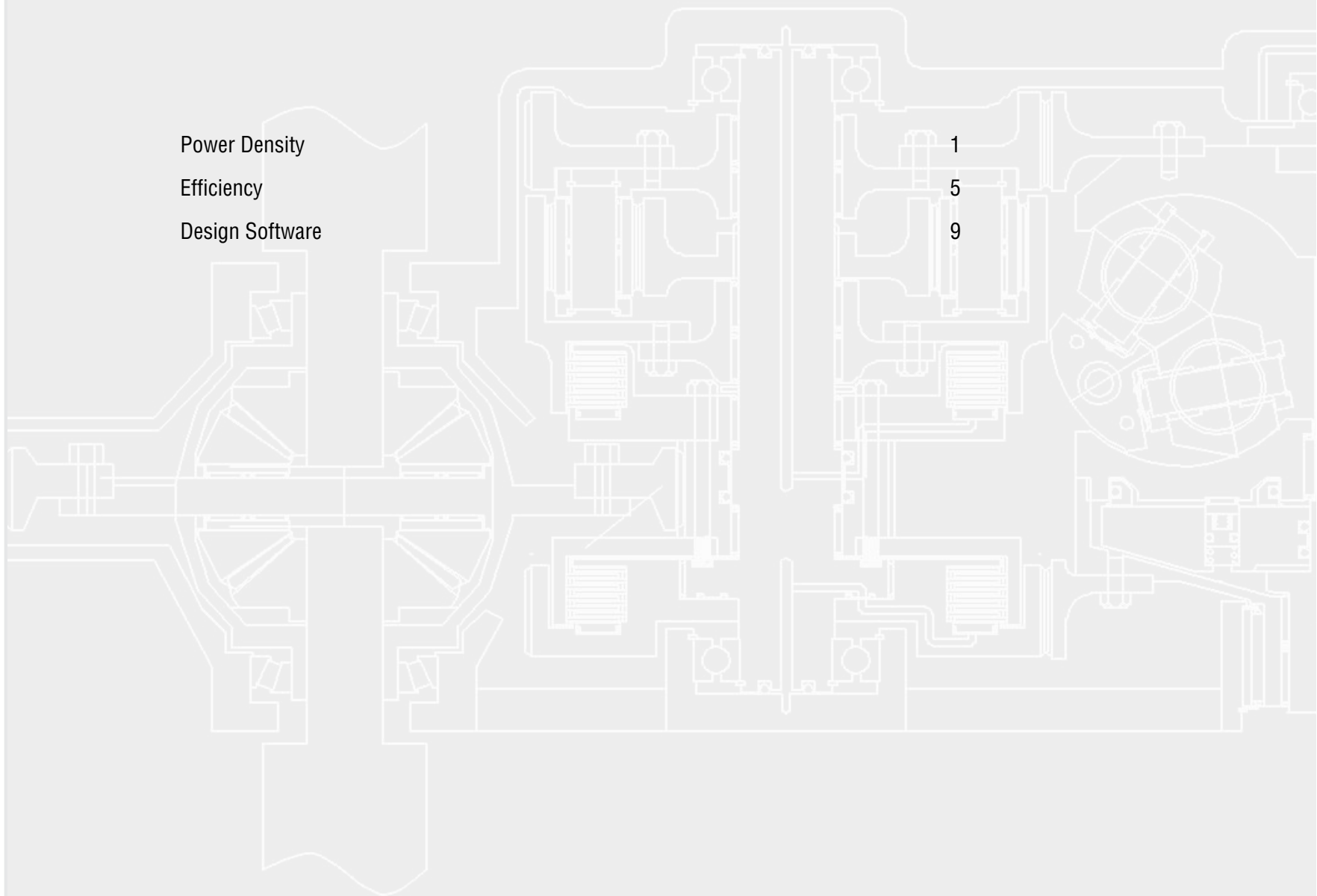


# Double Roller Full Toroidal Variator



Power Density  
Efficiency  
Design Software

1  
5  
9



# Power Density

The Power density of a DFTV is significantly higher than either the SFTV or the SHTV. It is also significantly higher than a similar capacity Push belt or Pull Chain CVT.

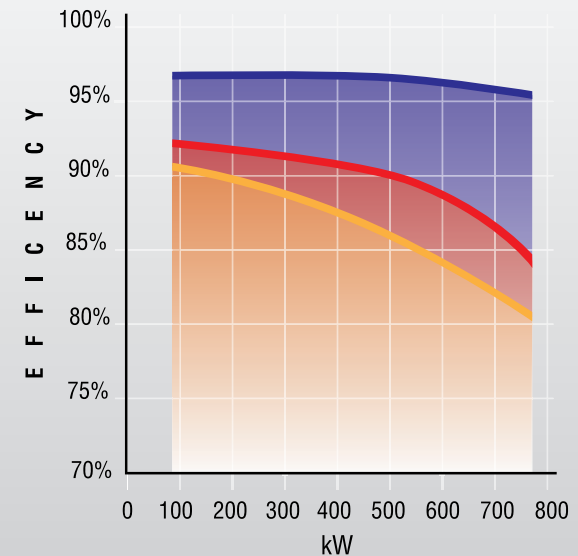
The diagram (right) maps the efficiency and input power envelopes for the three toroidal mechanisms. The efficiency and power density of a typical push belt CVT is similar to that of a SHTV.

A mathematical study of the power density of the DFTV design has been carried out that forms the basis of design software that can also be used to design working CVT's.

This study is comparative in nature using known design parameters used in the design of SFTV's and SHTV's.

The reasons for this improvement are explained in detail later in this paper.

Comparison of Efficiency and Power (kW) for 50kg Variator



Key

■ DFTV  
■ SHTV  
■ SFTV

1. A Variator of 50kg (Discs rollers and clamp only)
2. Operating at full power over a range of ratio
3. Using a traction coefficient of 0.05

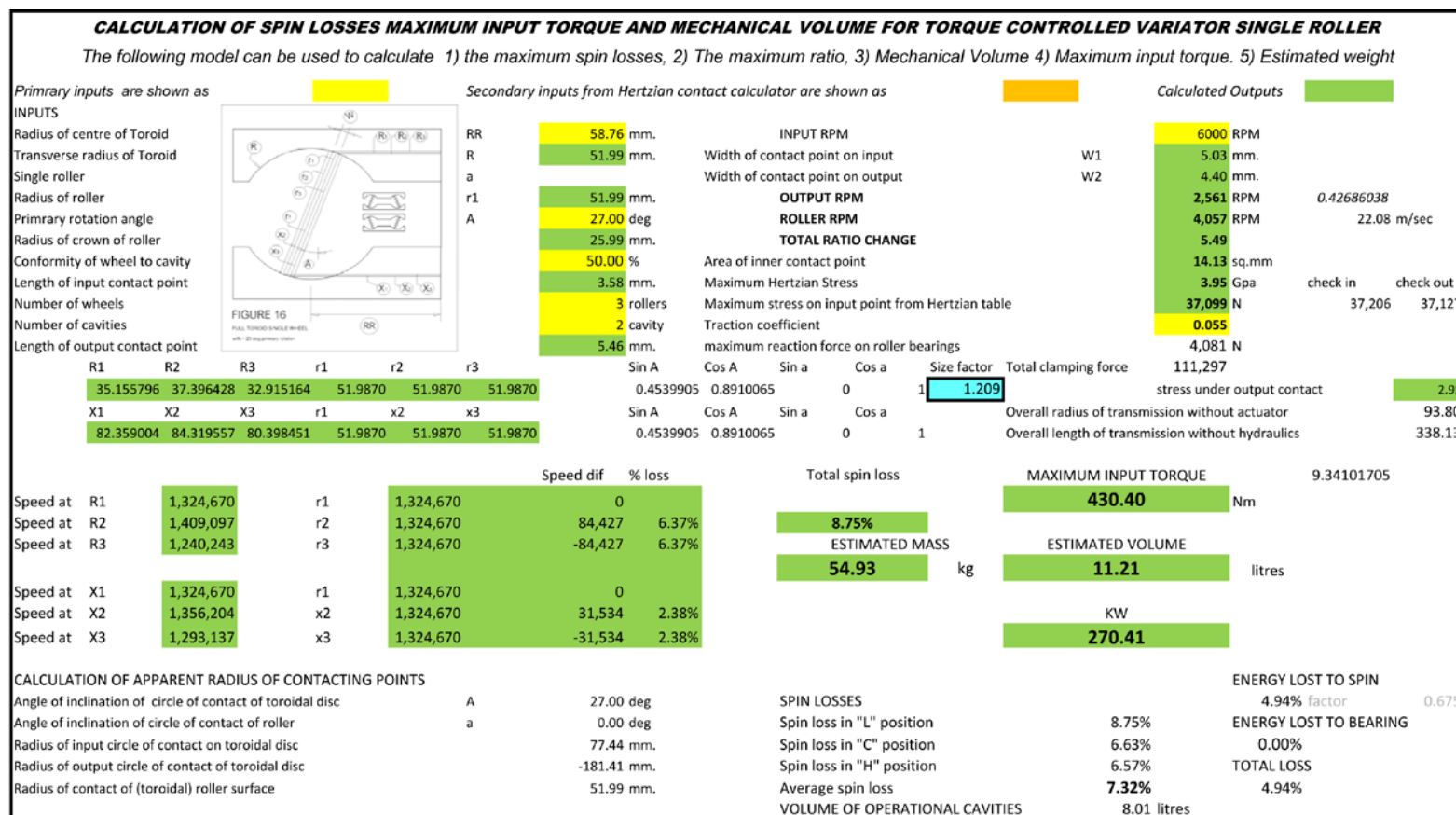
The reason for the dramatic improvement in power density is associated with four main factors. These all stem simply from the geometry of the DFTV design and have nothing to do with any new form of mechanical system or mechanical action.

1. Much larger contact patch area, allowing higher clamping forces and more torque transfer
2. Larger lever-arms that deliver higher torque values for the same clamping pressures.
3. More rollers within the cavity made possible because of their smaller size.
4. Greater conformity of contact radii made possible because of the inclination of the rollers to the central axis.

| CALCULATION OF SPIN LOSSES MAXIMUM INPUT TORQUE AND MECHANICAL VOLUME FOR TORQUE CONTROLLED VARIATOR DOUBLE ROLLER   |            |            |            |         |  |           |           |   |            |                        |             |   |                        |                |
|--|------------|------------|------------|---------|--|-----------|-----------|---|------------|------------------------|-------------|---|------------------------|----------------|
| The following model can be used to calculate 1) the maximum spin losses, 2) The maximum ratio, 3) Mechanical Volume 4) Maximum input torque. 5) Estimated weight |            |            |            |         |  |           |           |   |            |                        |             |   |                        |                |
| Primary inputs are shown as  |            |            |            |         | Secondary inputs from Hertzian contact calculator are shown as |           |           |   |            | Calculated Outputs     |             |   |                        |                |
| INPUTS   |            |            |            |         |  |           |           |   |            |                        |             |   |                        |                |
| Radius of centre of Toroid   |            |            |            |         | RR   | 67.07 mm. |           | INPUT RPM   |            |                        | 6000 RPM    |   |                        |                |
| Transverse radius of Toroid  |            |            |            |         | R  | 50.92 mm. |           | Width of contact point on input                   | W1         | 9.85 mm.               |             |   |                        |                |
| Wheel inclination  |            |            |            |         | a  | 21.70 deg |           | Width of contact point on output                  | W2         | 9.36 mm.               |             |   |                        |                |
| Radius of roller   |            |            |            |         | r1   | 24.80 mm. |           | OUTPUT RPM  |            | 2,561 RPM              | 0.42675328  |   |                        |                |
| Primary rotation angle   |            |            |            |         | A  | 31.95 deg |           | ROLLER RPM  |            | 9,707 RPM              | 25.20 m/sec |   |                        |                |
| Radius of crown of roller  |            |            |            |         |  | 38.70 mm. |           | TOTAL RATIO CHANGE                                |            | 5.49                   |             |   |                        |                |
| Conformity of wheel to cavity  |            |            |            |         |  | 76.00 %   |           | Area of inner contact point                       |            | 19.21 sq.mm            |             |   |                        |                |
| Length of input contact point  |            |            |            |         | L1   | 2.48 mm.  |           | Maximum Hertzian Stress                           |            | 3.85 Gpa               | check in    | check out   |                        |                |
| Number of wheels   |            |            |            |         |  | 4 rollers |           | Maximum stress on inner point from Hertzian table |            | 49,514 N               | 49,314      | 49,695  |                        |                |
| Number of cavities   |            |            |            |         |  | 1 cavity  |           | Traction coefficient                              |            | 0.055                  |             |   |                        |                |
| Length of output contact point   |            |            |            |         | L2   | 3.2016    |           | maximum reaction force on roller bearings         |            | 5,447 N                |             |   |                        |                |
|  | R1         | R2         | R3         | r1      | r2   | r3        | Sin A     | Cos A   | Sin a      | Cos a                  | Size factor | Total clamping force                              | 198,058 N              |                |
|  | 40.1211469 | 44.3014173 | 35.9408765 | 24.7986 | 26.6202  | 22.9770   | 0.529179  | 0.84851021  | 0.36974676 | 0.92913257             | 1.38        | stress under output contact                       | 3.17                   |                |
|  | X1         | X2         | X3         | r1      | x2   | x3        | Sin A     | Cos A   | Sin a      | Cos a                  |             | Overall radius of transmission without actuator   | 107.07                 |                |
|  | 94.0148531 | 97.9843536 | 90.0453526 | 24.7986 | 26.5283  | 23.0689   | 0.529179  | 0.84851021  | 0.36974676 | 0.92913257             |             | Overall length of transmission without hydraulics | 165.60                 |                |
|  |            |            |            |         |  |           |           |   |            |                        |             | Overall length between outside of discs           | 122.21                 |                |
|  |            |            |            |         |  |           | Speed dif | % loss  |            | Spin for this position |             | MAXIMUM INPUT TORQUE                              |                        | spin           |
| Speed at R1  |            | 1,511,765  |            | r1      | 1,511,765 mm/minute  |           | 0         |   |            |                        |             | 437.05  | Nm                     |                |
| Speed at R2  |            | 1,669,277  |            | r2      | 1,622,812  |           | 46,465    | 3.07%   |            | 5.83%                  |             |   |                        |                |
| Speed at R3  |            | 1,354,252  |            | r3      | 1,400,717  |           | -46,465   | 3.07%   |            |                        |             |   |                        |                |
|  |            |            |            |         |  |           |           |   |            |                        |             | ESTIMATED MASS                                    |                        |                |
|  |            |            |            |         |  |           |           |   |            |                        |             | 35.05   | kg                     |                |
|  |            |            |            |         |  |           |           |   |            |                        |             | ESTIMATED VOLUME                                  |                        |                |
| Speed at X1  |            | 1,511,765  |            | r1      | 1,511,765  |           | 0         |   |            | % of SFTV              |             | 4.40 Discs and rollers only                       | litres                 | torque density |
| Speed at X2  |            | 1,575,595  |            | x2      | 1,617,213  |           | -41,619   | 2.75%   |            | 63.82%                 |             | KW  |                        |                |
| Speed at X3  |            | 1,447,935  |            | x3      | 1,406,316  |           | 41,619    | 2.75%   |            |                        |             | 274.58  |                        |                |
| CALCULATION OF APPARENT RADIUS OF CONTACTING POINTS  |            |            |            |         |  |           |           |   |            |                        |             |   |                        |                |
| Angle of inclination of circle of contact of toroidal disc   |            |            |            | A       | 31.95 deg  |           |           |   |            |                        |             | 5.83%   | ENERGY LOST TO SPIN    |                |
| Angle of inclination of circle of contact of roller  |            |            |            | a       | 21.70 deg  |           |           |   |            |                        |             | 3.58%   | 2.23% factor           | 0.675          |
| Radius of input circle of contact on toroidal disc   |            |            |            |         | 75.82 mm.  |           |           |   |            |                        |             | 0.00%   | ENERGY LOST TO BEARING |                |
| Radius of output circle of contact of toroidal disc  |            |            |            |         | -177.66 mm.  |           |           |   |            |                        |             | 3.19%   | 0.00%                  |                |
| Radius of contact of (toroidal) roller surface   |            |            |            |         | 26.69 mm.  |           |           |   |            |                        |             | 7.17%   | TOTAL LOSS             |                |
|  |            |            |            |         |  |           |           |   |            |                        |             | 3.30%   | 2.23%                  |                |
|  |            |            |            |         |  |           |           |   |            |                        |             | Average spin loss                                 |                        |                |
|  |            |            |            |         |  |           |           |   |            |                        |             | VOLUME OF OPERATIONAL CAVITIES                    | 4.45 litres            |                |

Model of DFTV with input torque of 430Nm

Above is an extract from the mathematical model that maps all of these geometrical interactions in a DFTV and compares them to the geometry of a SFTV.



### Model of DFTV with input torque of 430Nm

It can be seen that the predicted torque density of this model for a DFTV is 187Nm/litre. This is compared to a SFTV at 38.4Nm/litre – Almost five times.

A similar analysis has been done for a SHTV.

## CALCULATION OF SPIN LOSSES MAXIMUM INPUT TORQUE AND MECHANICAL VOLUME FOR TORQUE CONTROLLED VARIATOR SINGLE ROLLER

### HALF TOROID

The following model can be used to calculate 1) the maximum spin losses, 2) The maximum ratio, 3) Mechanical Volume 4) Maximum input torque. 5) Estimated weight

Primary inputs are shown as

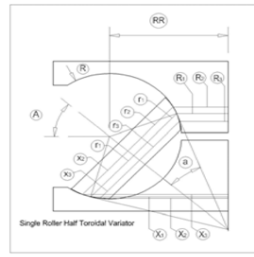
Secondary inputs from Hertzian contact calculator are shown as

Calculated Outputs

NOTE - It is possible to input without preparing a drawing provided the following rules are followed. The Roller radius is calculated after inputting the "included angle". The number of wheels can be inputted with some knowledge of the geometry. The number of cavities is a function of experience/life. The maximum allowable "spin" is related to acceptable values and in the case of the Half Toroid occurs in the centre position. The volume is calculated as Transverse radius of Toroid \* 2 \* X1 \* X1 \* π \* a Constant developed from real designs. The contact ellipse and maximum allowable stress are calculated using [http://www.tribology-abc.com/calculators/e2\\_2.htm](http://www.tribology-abc.com/calculators/e2_2.htm). The Mass is calculated as volume by a machine density of 4.9

#### INPUTS

Radius of centre of Toroid  
Transverse radius of Toroid  
Included angle  
Radius of roller  
Primary rotation angle  
Radius of crown of roller  
Conformity of roller to cavity  
Length of input contact point  
Number of rollers  
Number of cavities  
Length of output contact point



| R1        | R2          | R3      | r1      | r2      | r3      |
|-----------|-------------|---------|---------|---------|---------|
| 24.914374 | 26.52999104 | 23.2988 | 31.2549 | 33.2817 | 29.2282 |
| X1        | X2          | X3      | r1      | x2      | x3      |
| 66.741658 | 70.60621864 | 62.8771 | 31.2549 | 33.0647 | 29.4452 |

57.60 mm.  
35.04 mm.  
26.88 deg  
31.25 mm.  
42.00 deg  
28.03 mm.  
80.00 %  
2.09 mm.  
3 rollers  
2 cavity  
3.552 mm.

INPUT RPM  
Width of input contact point  
Width of output contact point

6000 RPM  
8.97 mm.  
8.01 mm.

OUTPUT RPM  
WHEEL RPM  
TOTAL RATIO CHANGE

2,240 RPM  
4,783 RPM  
5.36

Area of input contact point  
Maximum Hertzian Stress  
Maximum stress on input point from Hertzian table  
Traction coefficient  
maximum reaction force on roller bearings

14.73 sq.mm  
4.20 Gpa  
41,425 N  
0.070  
5,799 N

check in  
41,245  
check out  
41,523

Sin A  
Cos A  
Sin a  
Cos a  
Size factor  
Total clamping force

124,275 N  
stress under output contact

2.79

Reaction force on thrust bearing  
Overall radius of transmission without actuator  
Overall length of transmission without hydraulics  
Overall length between outside of discs

37454.6 N  
101.20  
227.9024  
168.192

#### Total spin loss

#### MAXIMUM INPUT TORQUE

| Speed at | R1 | R2      | R3 | r1 | r2      | r3 | Speed dif | % loss |
|----------|----|---------|----|----|---------|----|-----------|--------|
| Speed at | R1 | 938,774 |    | r1 | 938,774 |    | 0         |        |
| Speed at | R2 | 999,650 |    | r2 | 999,649 |    | 1         | 0.00%  |
| Speed at | R3 | 877,897 |    | r3 | 877,898 |    | -1        | 0.00%  |
| Speed at | X1 | 938,774 |    | r1 | 938,774 |    | 0         |        |
| Speed at | X2 | 993,132 |    | x2 | 993,131 |    | 0         | 0.00%  |
| Speed at | X3 | 884,416 |    | x3 | 884,416 |    | 0         | 0.00%  |

#### ESTIMATED MASS

92.54 kg

spin in this position

0.00%

#### ESTIMATED VOLUME

18.89 litres

5.41 Discs and rollers only

KW

272.34

litres torque den: 80.14951

#### SPIN LOSSES

Spin loss in "L" position  
Spin loss in "LM" position  
Spin loss in "C" position  
Spin loss in "HM" position  
Spin loss in "H" position  
Average spin loss

4.93%  
2.50%  
0.00%  
3.33%  
4.86%  
2.60%

ENERGY LOST TO SPIN  
5.20%

#### CALCULATION OF APPARENT RADIUS OF CONTACTING POINTS

|  |             |
|--|-------------|
| Angle of inclination of circle of inner contact    | 21.12 deg   |
| Angle of inclination of circle of outer contact    | 105.12 deg  |
| Angle of inclination of roller                     | 26.88 deg   |
| Radius of roller circle of contact                 | 35.04 mm.   |
| Radius of inner circle of contact on toroidal disc | 26.71 mm.   |
| Radius of outer circle of contact on toroidal disc | -255.82 mm. |

#### Model of SHTV with input torque of 430Nm

In this case the predicted torque density is 94.25Nm, However the predicted energy losses are much higher.

Torque density, life, and efficiency are so interrelated that it is not possible to make conclusions about one of them without checking what is happening with the other two.

It is very clear that the DFTV will always be much smaller than either a SFTV or a SHTV, when similar efficiencies and life are being designed for.



A Double Roller Full Toroidal Variator (DFTV) is perhaps the most efficient form of CVT available.

Typically the overall efficiency advantage of a DFTV over a Torotrak SFTV design is of the order of 8% -10%.

The efficiency advantages are brought about by

1. the reduction in velocity differences at the roller and disc contacts
2. the elimination of roller thrust bearings
3. the reduction in size of the hydraulics required to control ratios.
4. The fact that in a DFTV the discs both rotate in the same direction

**There is a tradeoff between efficiency and Power density.** It is possible to improve the efficiency of either a DFTV or a SFTV by decreasing the ratio of the crown radius of the rollers to the toroidal cavity so that the contact patch becomes narrower. However if the same power or torque capabilities are to be maintained the components must be larger and the power density reduces.

In the case of a SHTV decreasing the crown radius does not have such a dramatic affect on the power density because most of the energy lost is associated with the thrust bearing, the efficiency of which is not affected by a change in crown radius of the roller.

NSK have published a great deal of information on this subject and the chart below is a good example.

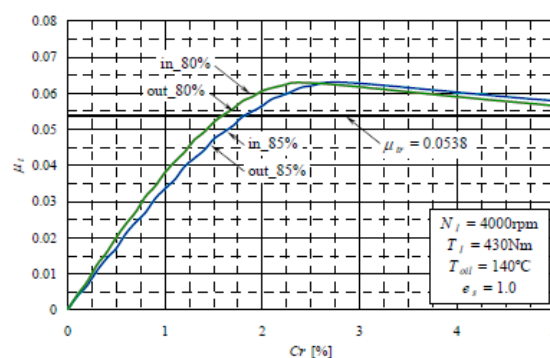


Fig.4 Comparison of power-roller curvature ratio of 80 and 85% on traction curves at  $e_s = 1$  and  $T_{oil} = 140^\circ\text{C}$

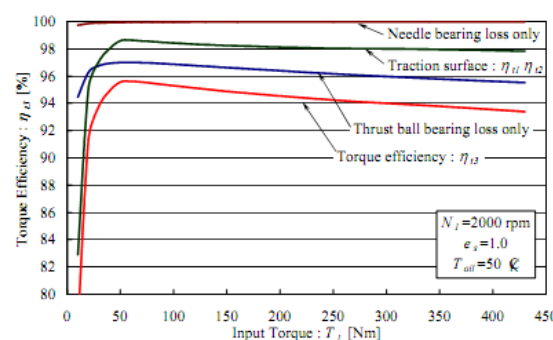
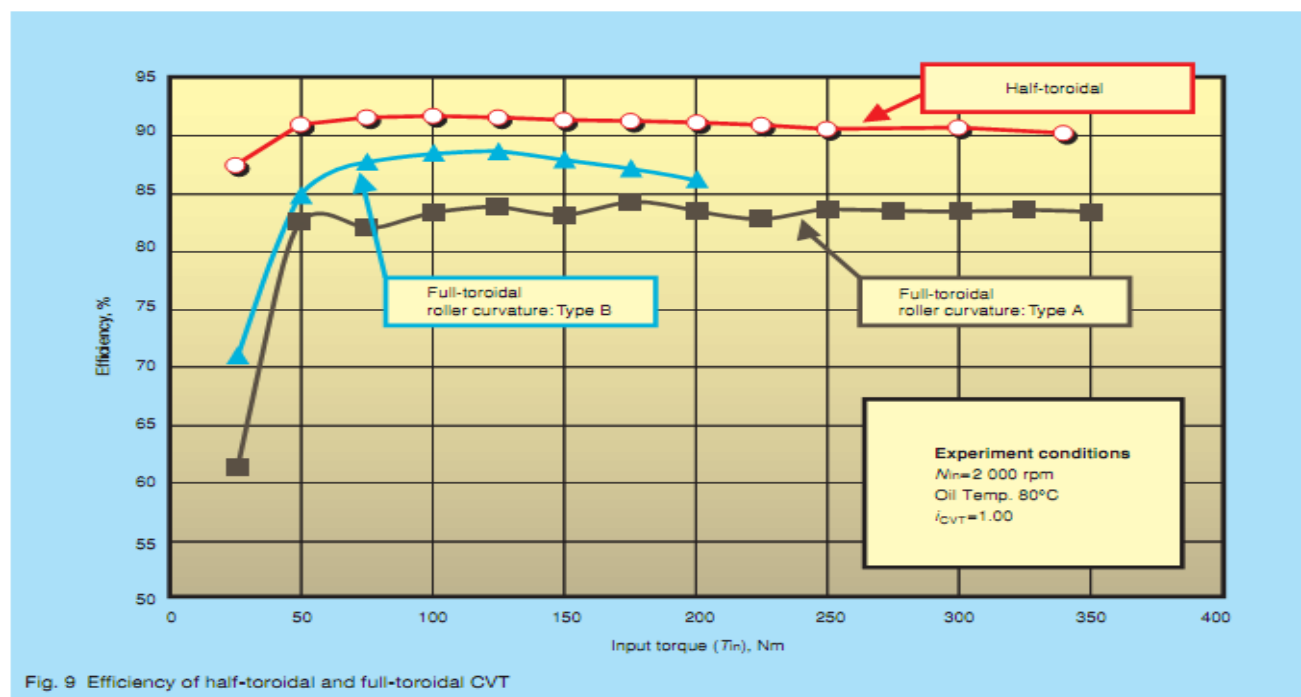


Fig.6 Calculated torque-transmission efficiency of the variator, and portion of torque losses of thrust ball-bearings, needle bearings and spin loss on the traction contact at  $e_s = 1$ ,  $N_f = 2000\text{rpm}$  and  $T_{oil} = 50^\circ\text{C}$

Extract from Paper "Development of a 6 Power - Roller Half - Toroidal CVT - Mechanism and Efficiency - " Hirohisa Tanaka & Nozomi Yoyoda Yokohama National University & Hisashi Machida, & Takashi Imanishi NSK Ltd.

NSK have also studied the relative differences between a **SFTV** and a **SHTV** efficiencies. They have also studied varying the crown radius in a SFTV and its affect on efficiency and power throughput. The chart below is also a good example of this work



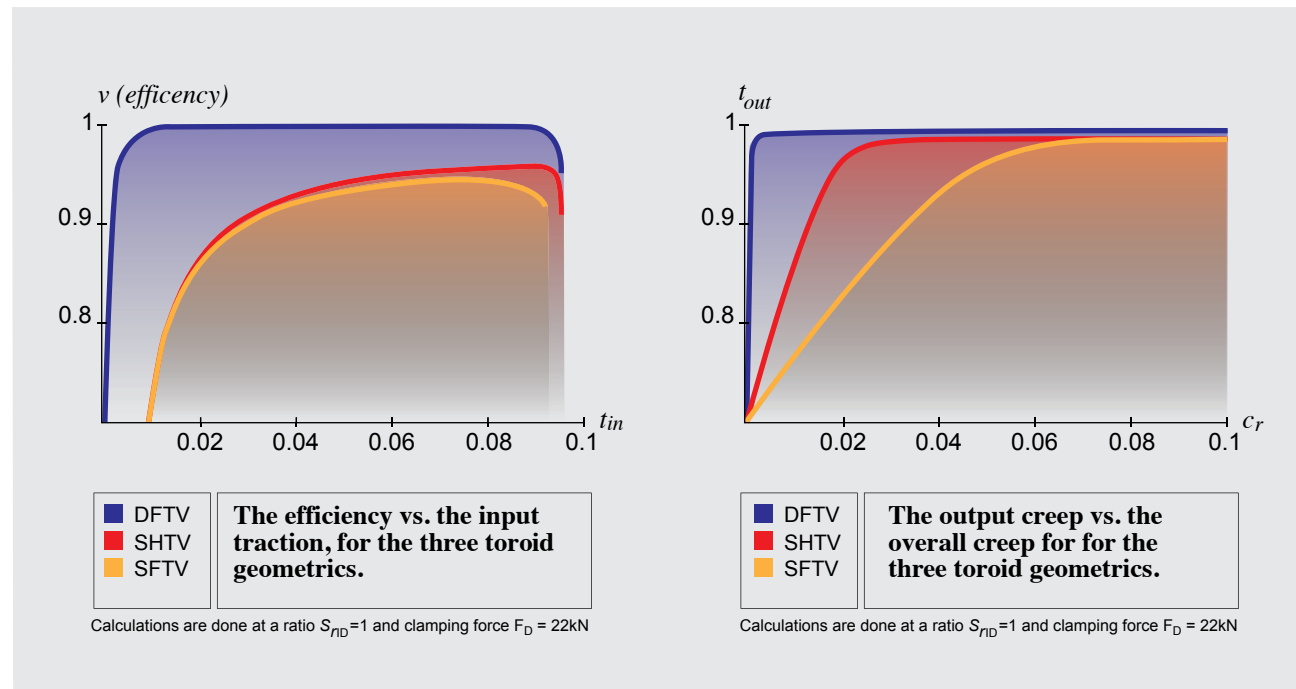
Extract from paper "Development of POWERTOROS Unit Half toroidal CVT – Comparison between Half-Toroidal and Full-Toroidal CVT's" Takashi Imanishi & Hishashi Machida Research and development Centre NSK.

Additional energy savings are associated with the fact that both the input and output discs rotate in the same direction for the **DFTV**.

With an input of 6,000RPM and a ratio spread of 4 the maximum differential rotational speeds of a DFTV are 6,000RPM in high gear with 3,000RPM in low , while that of a SFTV will be 18,000RPM in high gear and 9,000RPM in low.



The DFTV exhibits a significant improvement in efficiency over the SFTV and SHTV and almost zero creep when in the 1:1 ratio position. This is despite the existence of three power contacts.



These graphs depict the DFTV in its most efficient state which occurs over almost 60% of its ratio range. The DFTV exhibits an efficiency improvement over the SFTV of between 6% and 4.5% at all times.

In a DFTV and a SFTV no thrust bearings are required to support the rollers. In a SHTV although the geometric arrangement reduces the differential velocities it necessitates the thrust bearings, and these consume a great deal of energy.

In a DFTV the geometry reduces the differential velocities but leaves the system balanced with no need for thrust bearings.

In a SFTV the hydraulic system must move the rollers against the Torque reaction Force (TRF) a reasonable distance during a ratio change. In order for the ratio change to be executed quickly the hydraulic system must be reasonably large.

In a SHTV the arrangement is the same but the rollers only move a very small distance although this movement must be extremely fast or a ratio overrun will occur.

Calculations carried out by Ultimate Transmissions indicate that the energy consumption of a Torotrak control system will be of the order of 5%. Not enough information is available to study the SHTV. Although the ratio changing itself occurs over only small time frames, the hydraulic system is operating all the time. The system must also be sized so as to function properly at low RPM which means that at high RPM it continues to consume comparatively large amounts of power.

The ratio control of a DFTV can be executed by a very small stepper motor requiring an energy input of less than 0.1% of the input power. Virtually no force is required to execute a ratio change.

In a DFTV the input and output discs rotate in the same direction. In a SFTV and a SHTV they rotate in opposite directions.

This means that a simpler variator architecture can be adopted and far less parasitic losses associated with windage and oil churning are experienced.

The diagram right, maps the efficiency and power capabilities for the three mechanisms.

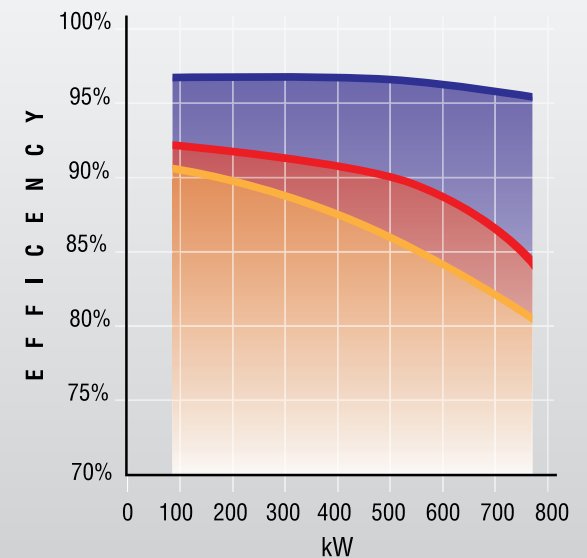
The typical power range for a SFTV or SHTV of this size is 300kW to 400kW or 400Nm at 6000RPM with a vehicle design life of 400,000kms.

This capability can be expanded beyond this by increasing the conformity of the roller to the toroidal discs.

The design range for a DFTV of 50 kg. is 800 kW. It cannot be expanded beyond this because the support bearings for the rollers become overstressed for this design life.

All variators can be increased in power by increasing the traction coefficient. The 0.05 used here is considered the most likely upper limit in real CVT's.

**Comparison of Efficiency and Power (kW) for 50kg Variator**



Key

■ DFTV  
■ SHTV  
■ SFTV

1. A Variator of 50kg (Discs rollers and clamp only)
2. Operating at full power over a range of ratio
3. Using a traction coefficient of 0.05

In order to design transmissions using the DFTV the operating parameters must first be established.

A relatively simple software has been produced by Ultimate Transmissions that enables these parameters to be established for all three toroidal variator types. By comparing the output parameters of all three some simple reverse engineering can be undertaken using working examples of the SFTV and the SHTV to fine tune or confirm the parameters predicted for the DFTV.

The software is based on this description and can be made available to any parties interested in more detailed evaluation.

## Designing Toroidal Variators using a Comparative Approach

**Single Roller Full Toroidal Variator (SFTV) Single Roller Half Toroidal Variator (SHTV) and Double Roller Full Toroidal Variator (DFTV)**

PREPARED BY MICHAEL DURACK FOR ULTIMATE TRANSMISSIONS

### Overview

Traction drives are one of the oldest forms of transmissions. They preceded gears as they were much simpler to make.

The first forms of traction drives used “dry” friction to transfer force from what was typically a roller on a disc that could change its position on the disc and so change ratio. Unfortunately dry friction is very prone to wear and these early drives required high levels of maintenance. Many smaller machines continue to use friction drives (as they were called) when gears, present particular mechanical problems.

*cont >*

## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

Modern high power traction drives use a fluid called a “Traction Fluid” to separate the rolling components so that no metal to metal contact occurs and wear is more or less eliminated. The traction fluid increases in viscosity by billions of times when subject to very high pressures and behaves like a glassy solid as the rollers roll over the disc.

The most successful of these are called Toroidal Variators. There are the three types - SFTV, SHTV, and DFTV.

The SFTV is promoted by companies like Torotrak ([www.torotrak.com](http://www.torotrak.com)) CVTcorp ([www.cvtcorp.com](http://www.cvtcorp.com)) while the SHTV by companies like Nissan and NSK ([www.nsk.com](http://www.nsk.com) under the brand name Powertoros).

The DFTV has been recently developed by Ultimate Transmissions and exhibits superior performance and greater power density.

Excel spreadsheets have been developed by Michael Durack for Ultimate Transmissions that can be used to calculate the key performance characteristics of Double Roller Full Toroidal Variators (DFTV) Single Roller Full Toroidal Variators (SFTV) and Single Roller Half Toroidal Variators (SHTV).

### **The key factors that control the ability of a Toroidal based CVT to transmit torque are**

- The maximum stress that the contact points on the rollers and discs can withstand.
- The Traction coefficient of the Traction Fluid
- The degree of differential velocities present at the contact points.

These excel spread sheets calculate with a reasonable level of certainty the relationship of these three variables within the three different mechanisms, and allow designs to be produced rapidly.

## Basic Inputs

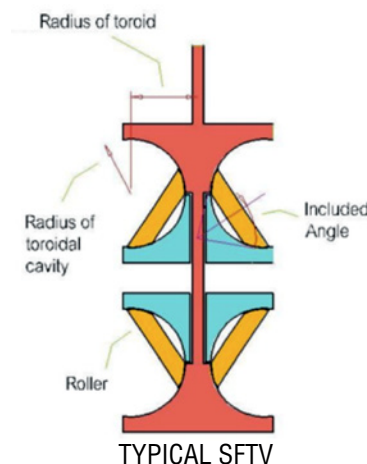
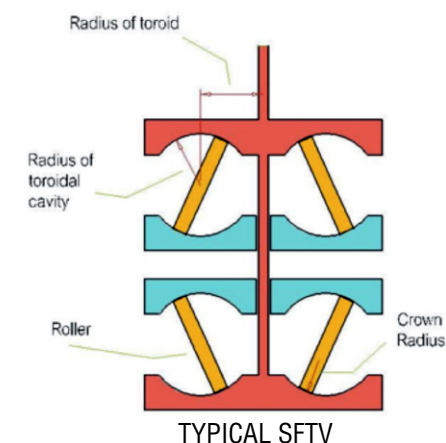
In all three cases these spreadsheets rely on the following basic inputs. These inputs are shown as yellow in the spread sheets. They are inputted into the sheet referred to as DFTV L, SFTV L and SHTV L. It should be noted that the DFTV and SFTV models are in the same work book.

*cont >*

## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

1. The Radius of the Toroidal cavity (R)
2. The Radius of the Toroid (RR)
3. The Radius of the roller (r1). This number applies only to the DFTV and the SFTV. The roller radius for the SHTV is derived from R and Cos of the “included angle” a.
4. The relationship of the crown radius of the roller to the toroidal cavity radius as a percentage. This relationship is often referred to as the crown radius conformity. (c)
5. The Number of cavities. (NC)
6. The number of rollers (or roller pairs DFTV) in each cavity. (NR)
7. The (Design) Traction coefficient. (TC)
8. The maximum contact pressure allowed at the contact of the roller with the discs. (MH)
9. The maximum input RPM. (IRPM)
10. The Primary Rotational Angle or the angle of rotation that determines the gear ratio operating inside the Variator. (A). This angle is zero in the centre and either positive or negative on either side of this.

In the case of the DFTV and the SHTV there are two secondary geometric inputs that are designed to generate zero (or close to zero) spin, or zero differential velocities at the roller contacts for some positions. It is not possible with the SFTV to arrange this in any position.



cont >

## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

11. The Roller Inclination (a). For DFTV only. This represents the angle formed between the roller axis and the centre line or conical contact line, where the two cones contact each other. At a certain angle it is possible to ensure no spin or differential velocities occur at the contact patch in one position. This position is usually arranged to happen in the 1:1 ratio or centre position.
12. The Included angle (a). For SHTV only. This represents the angle formed by the tangent line at the contact point and the centre of rotation of the roller. At a certain angle it is possible to ensure no spin or differential velocities occur at the contact patches in at least one position. This position is usually arranged at the extreme speedup or slow down positions.

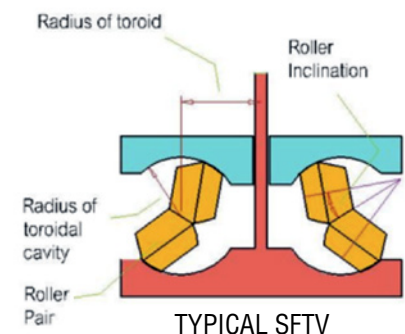
All of the lengths inputted in this first step can be scaled up using a "Size factor". This size factor can be entered manually to automatically scale up all lengths areas and performance outputs. This is shown in blue in the spread sheet.

## Secondary Geometric Outputs

A number of geometric outputs are calculated (using the Basic Inputs) that determine the contact radii of the points of contact. It is necessary to calculate these radii accurately so that the properties of the elliptical Hertzian contact points can be established accurately.

These are shown as an olive colour in the spread sheets.

Firstly the contact radius of the roller is calculated (in the section CALCULATION OF APPARENT RADIUS OF CONTACTING POINTS ) in the spread sheet. Using the following formulae.



cont >



## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

### **$rr = r1/\cos aa$ where**

- $rr$  is the Actual Radius of contact of (toroidal) roller surface
- $r1$  is the radius of the roller where it contacts the disc
- $aa$  (in the case of the SFTV) is the Angle of inclination of the roller plane of rotation to the line connecting the contact point to the centre of the toroidal cavity in the case of the SHTV it is the angle (also  $aa$ ) between the plane of rotation of the roller and the plane containing the tangents of the contact patch

In the case of the SFTV the angle  $aa$  is zero so the contact radius is the same as the actual radius, whereas for the other two the contact radius is larger than the actual radius.  $rr$  is the same for either the input and output contact and remains the same for any ratio.

Secondly the radius of the input and output contacts on the discs are calculated (again located in the section CALCULATION OF APPARENT RADIUS OF CONTACTING POINTS ) in the spread sheet, using the following formulae. The input and output contacts are different except for the centre position where they are both the same.

### **$RI = R1/\sin A$ where**

- $RI$  is the Actual Radius of the contact circle of the disc to the roller at the input contact point.
- $R1$  is the distance of the input contact patch to the centre of rotation of the discs.
- $A$  is the angle of rotation (ratio) of the roller or rollers.

### **$RO = X1/\sin A$ where**

- $RO$  is the Actual Radius of the contact circle of the disc to the roller at the output contact point.
- $X1$  is the distance of the ioutput contact patch to the centre of rotation of the discs.
- $A$  is the angle of rotation (ratio) of the roller or rollers.

For both the SFTV and the DFTV at the centre position (1:1) the radius is infinite. Generally the outside contact point in both the SFTV and DFTV is a negative number. In the case of the SHTV only the extreme outer point may be negative.

For the SHTV the following formulae are used. This requires two steps first to calculate the angles of inclination of the circle of contact for the input and output and to then apply it to the contact radii on the discs.

*cont >*

## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

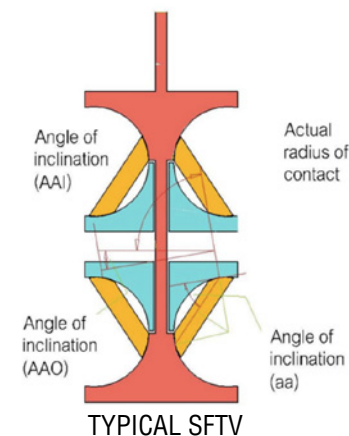
### Step 1

$AAI = 90 - aa - A$  where

- $AAI$  is the angle of inclination of the input contact circle to the direction of the roller reaction
- $aa$  is the included angle
- $A$  is the primary rotational angle

$AAO = 90 - aa + A$  where

- $AAO$  is the angle of inclination of the output contact circle to the direction of the roller reaction
- $aa$  is the included angle
- $A$  is the primary rotational angle



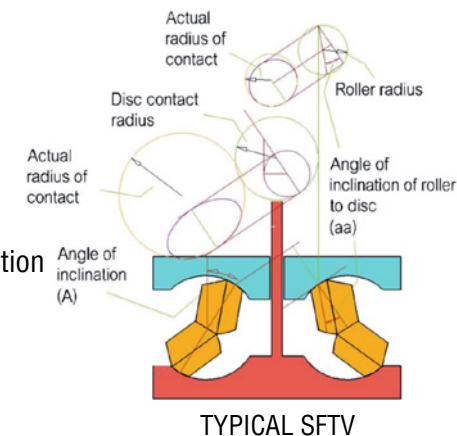
### Step 2

$RI = R1 / \cos AAI$  where

- $RI$  is the radius of the contact circle of the disc to the roller at the input contact point.
- $R1$  is the distance of the input contact patch to the centre of rotation of the discs.
- $AAI$  is the angle of inclination of the input contact circle to the direction of the roller reaction

$RO = X1 / \cos AAO$  where

- $RI$  is the radius of the contact circle of the disc to the roller at the input contact point.
- $R1$  is the distance of the input contact patch to the centre of rotation of the discs.
- $AAO$  is the angle of inclination of the output contact circle to the direction of the roller reaction



cont >

## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

The actual crown radius is calculated using this formula

**$cr = R \times c$  where**

- $cr$  is the actual crown radius of the roller
- $R$  is the radius of the toroidal cavity
- $c$  is the crown radius conformity

### Secondary Inputs

Once all of the contact radii have been calculated it is possible to calculate the maximum force that the rollers can exert on the discs. This is done using a Hertzian contact stress calculator ensuring that the maximum Hertzian stress (inputted earlier) is not exceeded.

Using this calculator the following inputs are derived. These are then manually entered into the appropriate field shown brown in the spread sheet.

- Maximum force for the input point (MF)
- Width of the contact point at the input point (W1)
- Length of the contact point at the input point (L1)

The calculation is repeated for the outer contact using the same maximum force but the new contact radii appropriate for that point, and the following inputs are derived

- Maximum stress at the output point (MHS)
- Width of contact point at the output point (W2)
- Length of contact point at the output point (L2)

Generally the stress is lower at the output point and the contact patch longer and narrower because of the different contact radii.

It is important when calculating the patch width and length of the SFTV that the correct number is applied to the contact patch. Generally the SFTV contact patch is longer than it is wide, whereas the contact patch for the other two is almost always wider than it is long. This is simply the result of using closer conformity rollers in the SHTV and the DFTV than in the SFTV.

*cont >*

**DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH**

## Calculated Torque Rpm & Spin (Low Gear)

The model now calculates the maximum input torque. It is always assumed that this occurs at extreme low gear and will be the ultimate limitation placed on the CVT. The maximum input torque is calculated using this formula

**Maximum input torque = NC x NR x MF x TC x R1 where**

- NC is the number of cavities
- NR is the number of rollers or roller pairs in the CVT
- MF is the maximum reaction force on the roller disc contact
- TC is the traction coefficient
- R1 is the radius of the input contact to the centre of rotation of the discs.

R1 is calculated by using this formula

**R1 = RR - R x SIN A where**

- R1 is the input radii
- RR is the radius of the toroid
- R is the radius of the toroidal cavity
- A is the angle of rotation of the roller

The output RPM is calculated using this formula

**ORPM = IRPM x R1/X1 where**

- IRPM is the input RPM
- ORPM is the output RPM
- R1 is the input radii
- X1 is the output radii

*cont >*

## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

The model now calculates the surface velocities of the extreme outside edges of the contact patch.

It firstly calculates the rotational radii on the disc at the contact patch and the roller at the contact patch using the basic formulae for the disc and roller

**$R2 = R1 + W1/2 \times \cos A$  where**

- $R2$  is the outside edge (or faster edge) of the patch on the disc
- $W1$  is the width of the contact patch
- $A$  is the angle of rotation

**$r2 = r1 + W1/2 \times \sin a$  where**

- $r2$  is the matching edge to  $R2$
- $W1$  is the width of the contact
- $a$  is the angle of inclination of the rollers

It now calculates the speed of the surfaces at the edges and centre of both the input and output the contact patches. Firstly it calculates the speed of the centre of all of the patches using this formula.

**Speed at  $R1 = R1 \times 2 \times \pi \times \text{IRPM}$  where**

- $R1$  is the input contact radius
- $\text{IRPM}$  is the Input RPM

The Roller RPM ( $\text{RRPM}$ ) can now be calculated using this formula

**$\text{RRPM} = \text{Speed at } R1 / r1 / 2$  where**

- $r1$  is the radius of the roller

It now uses the other contact radii to calculate the speeds at the outer most points of the contacts.

It calculates the difference in speed for the outer edges of the input and output points and expresses it as an (absolute) percentage of the average speed. The four percentages are summed and divided by two. The division by two is simply because this method causes four numbers to be summed when in reality there are only two.

*cont >*

## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

### Calculation of Actual Energy Loss Associated with Calculated Spin Percentage for Low Gear

A study of energy losses disclosed by NSK in published data of the SHTV and this model indicates that the percentage should be factored by 0.675 to have it align with actual efficiency losses quoted by NSK for the “spin” only.

This factor is approximately 1/2 which would represent the relationship of the average pressures under the patch to the maximum pressure.

This constant also relates closely to the efficiency losses calculated by Professor Carbone for the DFTV and the SFTV.

### Calculation of Output Data for Other Gear Ratios

The models also create the performance characteristics for other gear ratios.

For the DFTV and SHTV these ratios are

- High gear which is set as the mirror of Low gear with A simply the negative value of the value of A for low gear. Referred to as DFTV H, SFTV H, and SHTV H
- The 1:1 ratio or central position where A equals zero. Referred to as DFTV C, SFTV C, SHTV C.
- A ratio called DFTV LM and SHTV LM – meaning Medium Low. There is no ratio for the SFTV. This ratio is such that the output speed is approximately half way between the Low Gear position and the central position.
- A ratio called DFTV HM and SHTV HM. There is no ratio for the SFTV. This ratio is such that the output speed is approximately half way between the High Gear position and the central position. It is the mirror of the Low Medium gears.

The Alternative ratios first calculate the amount of force that the roller must be subjected to in order to create the same level of input torque but inputted to the new radius for that ratio. The following formula is used to calculate this force.

*cont >*



**DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH**

**MF = Maximum Input torque / NR / NC / TC / R1 where**

- MF is the force required for that position
- NR is the number of rollers
- NC is the number of cavities
- TC is the traction coefficient used for low gear.
- R1 is the input radius for that gear ratio

This force is then used to calculate the maximum Hertzian stress and size of the input and output contact patches.

The spin losses can then be calculated as for Low Gear.

The process is repeated for the other gear ratios and a complete picture of stresses, energy losses, and output RPM's is created.

The Total Ratio Change (or spread) TRC is calculated simply by dividing the output RPM at High Gear by the output RPM at low gear.

## Calculation of Overall Energy Losses Due to Spin

With the spin loss for each ratio position calculated it is possible to create an average loss assuming that the CVT duty cycle uses each ratio an equal amount of time.

The SFTV has only three ratios calculated because the energy losses are similar for each ratio so the formula is simply:

Average spin loss = (Spin loss in L position + (Spin loss in C position x 2) + Spin loss in H position)/4

For the other the formula is as follows

Average spin loss = (Spin loss in L position + loss in LM position + (loss in C position x 2) + loss in HM position + loss in H position)/6

From this the actual energy loss due to spin can be calculated using the factor described earlier.

*cont >*

## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

Many other factors affect the final physical size of a working CVT and this figure can only be used as a guide to determine likely outcomes as a theoretical design is brought up to the status of a working mechanism.

### Other Volumetric & Weight Outputs of the Models.

Conceptual autocad drawings of working SFTVs SHTVs and DFTVs have been prepared. These have produced fractional relationships to the fundamental geometries of the three mechanisms. These are then used to create real volumetric and weight comparison, for mechanisms with the same maximum torque and similar efficiencies.

- Overall radius of the transmission without actuator
- Overall length of the transmission without hydraulics
- Overall length between the outside of the discs
- Estimated volume of the operational transmission
- Estimated weight of the transmission (a standard density of 4.9 is used to convert volume to density in all cases.)
- The fractional weight of the DFTV when compared to the other two

Generally the DFTV remains around 30% of the weight and volume of the other two, while also remaining a few percentage points more efficient.

### Other Operational Outputs of the Models.

The models also produce other operational numbers that can be used to assist with design such as –

- The torque reaction force on the rollers that must be supported by the roller bearing system.
- The maximum roller RPM
- The Maximum stress cycles on the rollers per minute
- The maximum differential speeds over the contact points.
- The area over which the heat generated by spin is distributed over the rollers.

*cont >*

## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

- The area over which the heat generated by spin is distributed over the discs
- The worst case energy loss at the contact patch
- The time spent by a point on the contact patch while being heated (assumes maximum torque input in low gear position)

Generally the SHTV contact patches experience around 25%- 50% of the heating intensity as that experienced by the SFTV. The area over which the heat is generated is larger and the spin intensity less than half. The DFTV is somewhere in the middle with greater area on the rollers and less time spent by the patch in the heating zone, but with more than twice the spin.

A separate calculation is carried out to determine the maximum Hertzian stress on the conical contact patches for the DFTV only.

A separate Sheet is included in the SHTV work book that calculates some of the operational characteristics of the thrust bearing. Although the detailed geometry of this thrust bearing is not known the calculations can be used to develop an understanding of the correlation of the likely energy loss on these bearings and the efficiency losses reported by NSK and Carbone.

## Calculation Of Actual Traction Coefficient (For DFTV Only)

A separate set of calculations is added to the DFTV calculations that take account of the ability of the DFTV to be designed using a direct relationship between the Torque reaction experienced by the rollers and the clamping force.

It is intended that the design of the DFTV includes a clamping system that is generated as a direct multiple of the torque reaction on the rollers.

The SFTV and the SHTV use other forms of clamping control that attempt to create a situation where “over clamping” is avoided.

The DFTV is unusual in that the areas of greatest spin occur at the high and low ends of the gear ratio range. The SHTV is the opposite and the SFTV remains with levels of spin that are similar over the whole range of ratios.

A simple clamping system that simply multiplies the roller torque reaction by the inverse of the traction coefficient can be used by all three mechanisms. In the centre position this relationship holds true, however as the rollers move away from the centre position the “wedging” action of the toroidal cavity will cause the actual roller reactions on the disc to increase by the inverse of the COS of the rotated angle.

*cont >*

## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

This increase in clamping force along with the reduction in Traction Coefficient suits the DFTV but not the other two. As the rollers move away from the centre (zero spin) position while the clamping force remains a multiple of the torque reaction on the rollers the actual force of the roller onto the disc increases by a factor equal to the inverse of the COS of how much the rollers are rotated.

Conversely the designer can select a traction coefficient that is selected as the highest possible (less a safety factor) for a contact patch experiencing the worst case spin, and using a particular traction fluid and operating at a predicted temperature. The model will then check how much the traction coefficient will need to increase as the rollers rotate towards the centre position.

A great deal of information is readily available on the “safe” traction coefficients for different levels of spin and temperature. The “unclamping” traction coefficient is thus reported as the “Actual clamping coefficient” In a typical DFTV this may move from 0.055 in the worst spin condition (>6%) to 0.065 when in the centre position with zero spin.

Although this relationship of spin and  $1/\text{COSA}$  may not give a perfect platform for minimizing over-clamping it is simple and robust.

## Selection Of Key Operational Limits When Designing A Dftv

The two key factors in setting the operational limits when designing a DFTV are

- 1. Maximum Hertzian Stress**
- 2. Traction Coefficient**

The most successful toroidal variator is undoubtedly the NSK SHTV. These transmissions have generally given reliable service in real vehicles of over 400,000 kms. It is believed that the most common failures were associated with the thrust bearings not the rollers and discs.

Without all of the design details it is not possible to understand exactly how this was done. However a detailed study of a (real) NSK SFTV transmission would allow reverse engineering that would uncover more accurately what limits of these two factors were used in the design.

A study of published NSK academic papers lead to the conclusion that they were as follows

1. 3.95GPa maximum stress or 2.63 GPa average
2. 0.055 in the centre position ( 4% spin) with over-clamping occurring in most other positions.

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## DESIGNING TOROIDAL VARIATORS USING A COMPARATIVE APPROACH

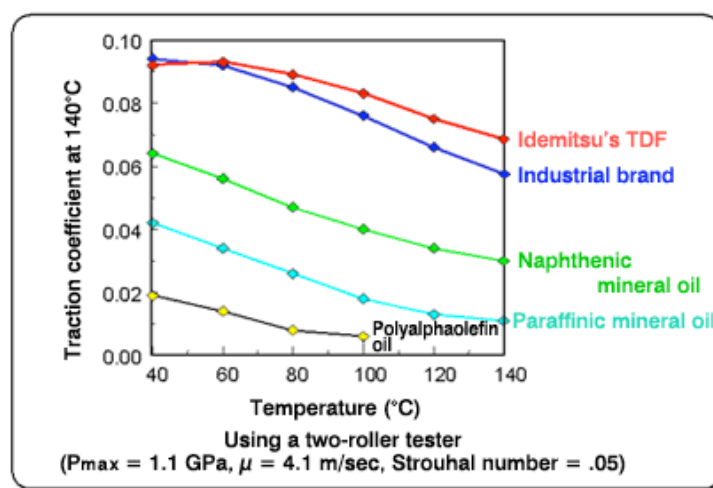
A study of Torotrak information is very confusing but it seems more like

1. 4.2 GPa or 2.8 average
2. 0.07 in the centre position (>6% spin ) with all other positions less than 0.07.

It is highly likely that the 0.07 coefficient quoted by Torotrak is unrealistically high in order to reduce the apparent size and weight of their transmissions.

This is particularly true when you consider that the contact patch in a Torotrak Variator may be 20 -30 degrees hotter than the patch in a NSK variator.

## Traction Coefficient Comparison



NSK use an Idemitsu Traction fluid that states its traction coefficients according to the above chart.

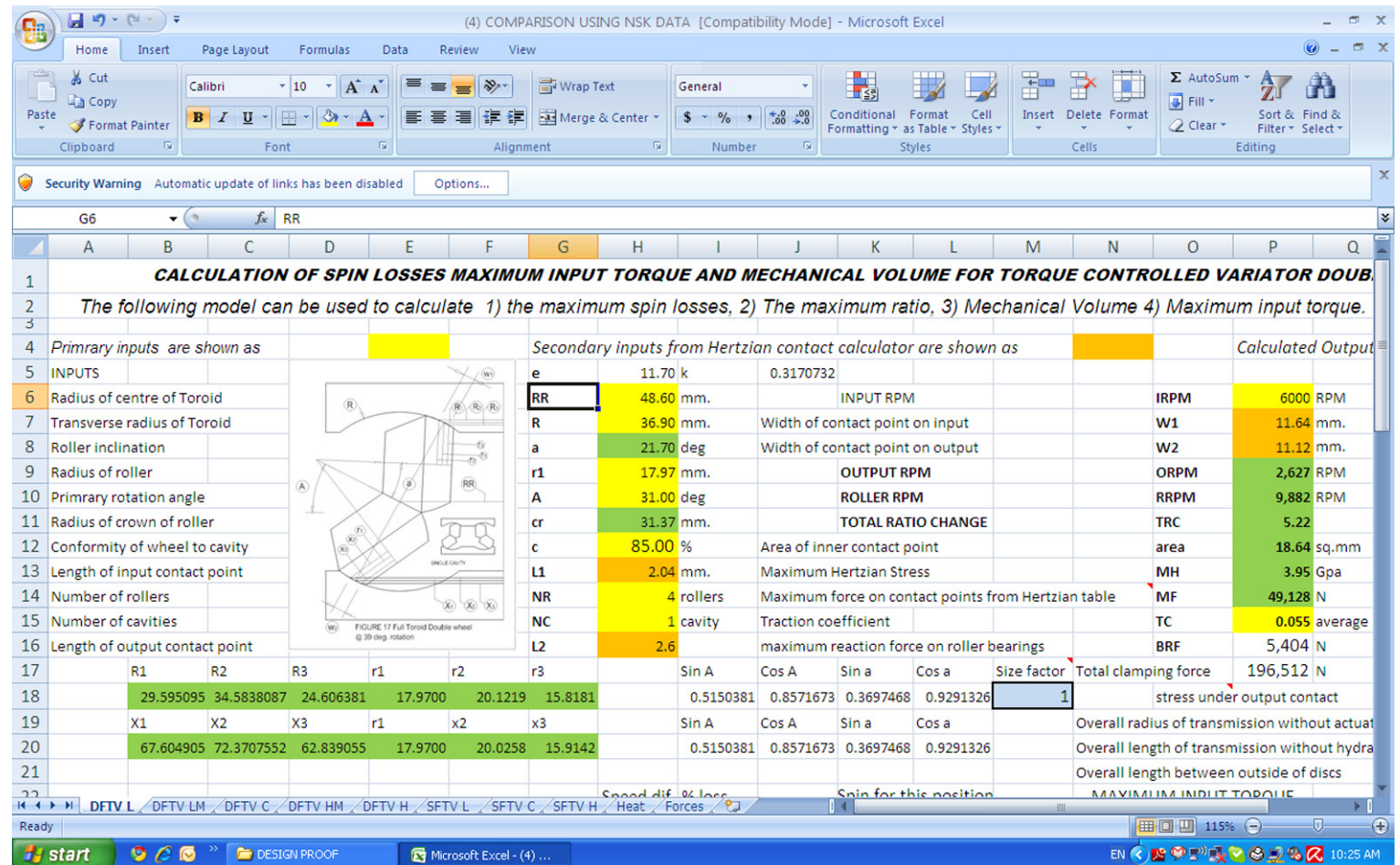
Torotrak use Santotrak fluids that are nowhere as well defined as Idemitsu when it comes to temperature affects.

If the traction fluid temperature is running at 160 degrees then using 0.07 would be very unsafe, particularly with a fluid with less quality than the Idemitsu fluid.

Any gross slip that might occur in Low gear will immediately damage the roller surface and the disc in the region of low gear.

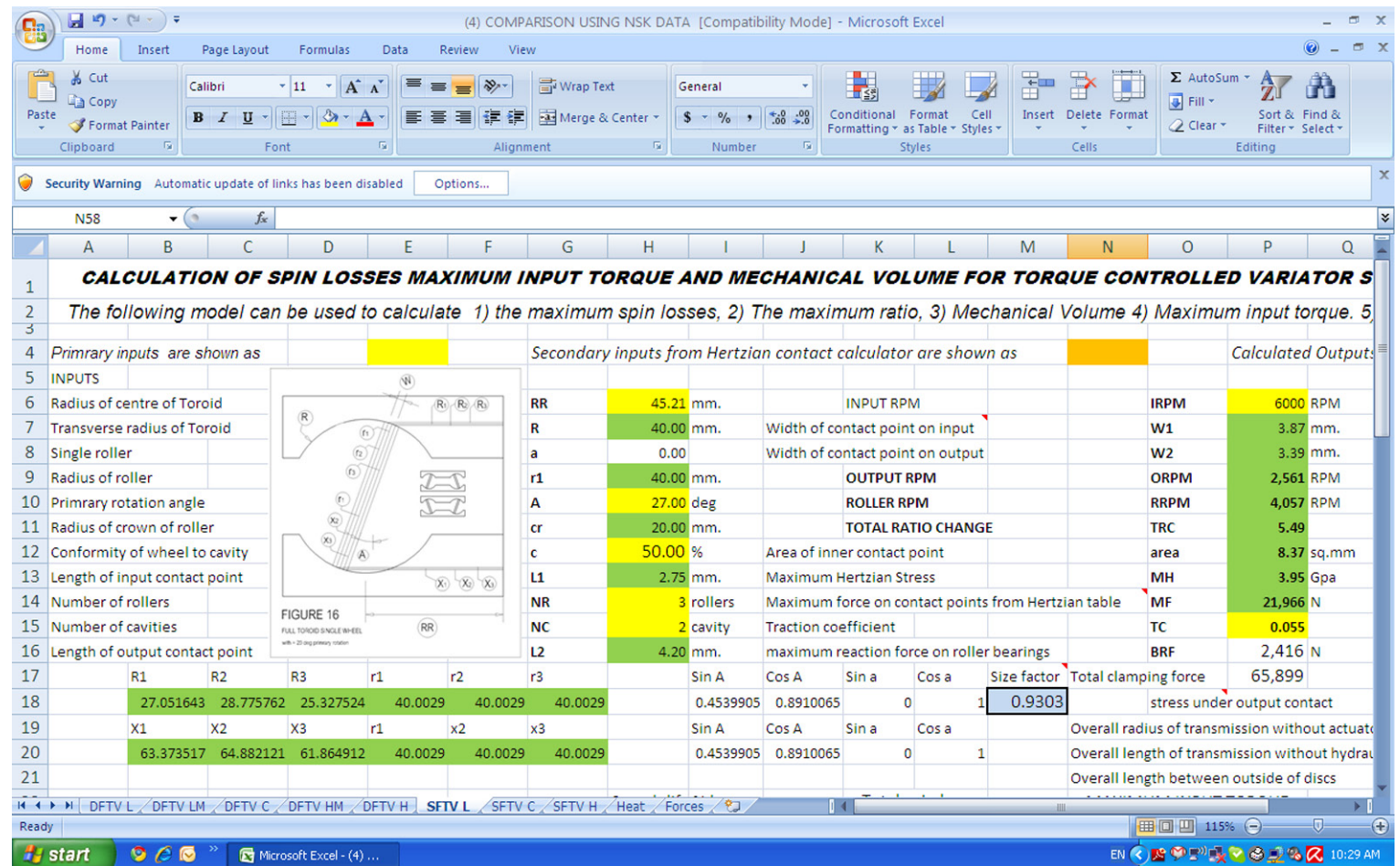
Torotrak's figure (differential velocity) in the worst case at 6,000RPM is 2.47 m/sec while NSK is 0.52 m/sec and the DFTV is 1.79 m/sec.

Below is a typical output pages derived from this software for the three toroidal types.

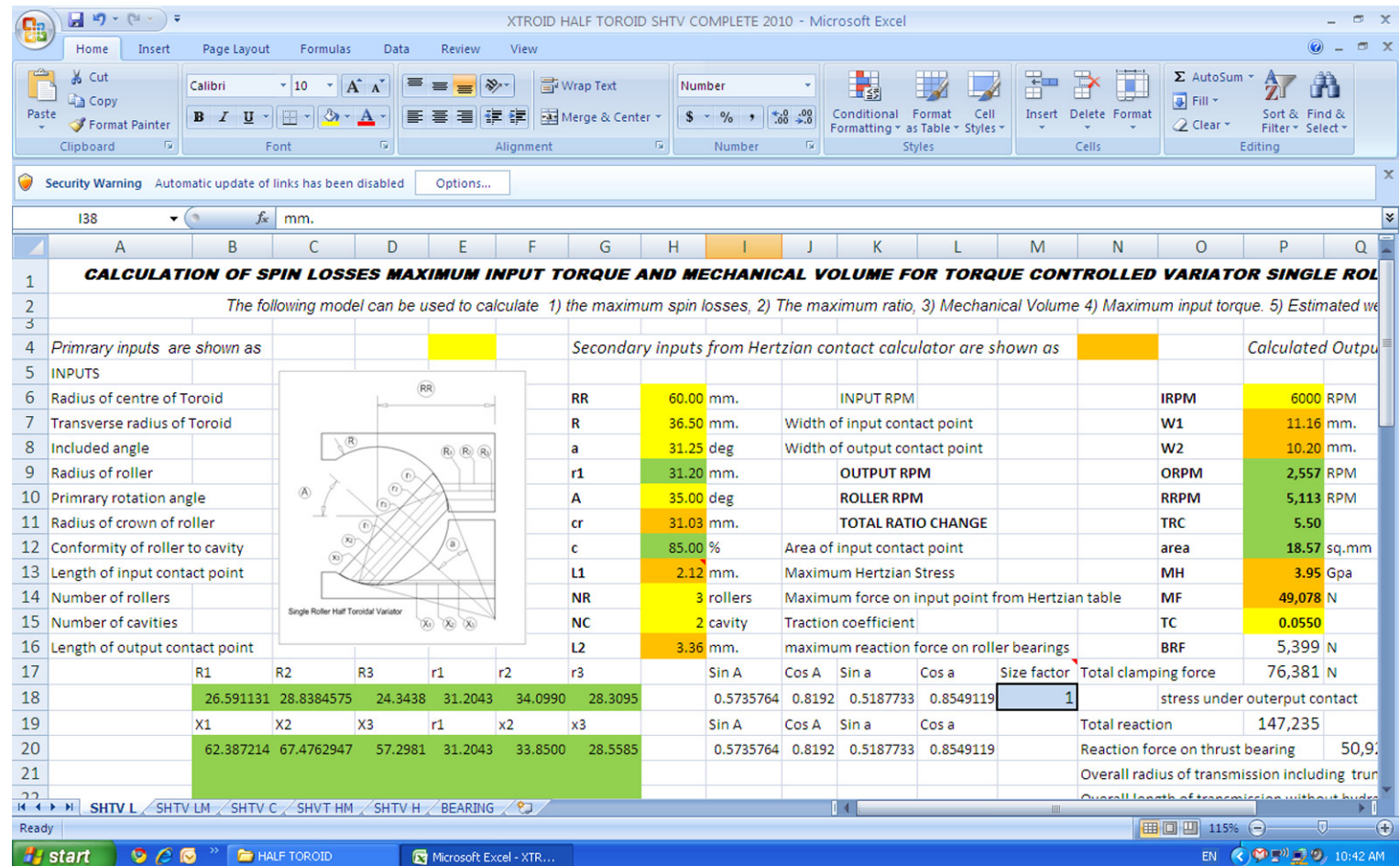


DESIGN PARAMETERS FOR DFTV WITH MAXIMUM POWER THROUGHPUT OF 270Kw





DESIGN PARAMETERS FOR SFTV WITH MAXIMUM POWER THROUGHPUT OF 270Kw



DESIGN PARAMETERS FOR SHTV WITH MAXIMUM POWER THROUGHPUT OF 270Kw

